

20. Calculate correct to six places of decimals.

$$(1.01)^{3/2} - (0.99)^{3/2}.$$

21. Sum the series to infinity :

$$\frac{5}{1!} + \frac{7}{3!} + \frac{9}{5!} + \dots$$

22. Sum to n terms of the series

$$3.5.7 + 5.7.9 + 7.9.11 + \dots$$

4186/M11

MAY 2010

Paper I — CALCULUS AND CLASSICAL ALGEBRA

(For those who joined in July 2003 and after)

Time : Three hours

Maximum : 100 marks

SECTION A — ($8 \times 5 = 40$ marks)

Answer any EIGHT questions.

1. If $y = \frac{1}{(x+1)(2x-1)}$, find y_n .
2. At which point is the tangent to the curve $x^2 + y^2 = 5$ parallel to the line $2x - y + 6 = 0$.
3. Find the radius of the curvature of the curve $x^4 + y^4 = 2$ at the point $(1, 1)$.
4. Show that $\int_0^{\pi/4} \log(1 + \tan \theta) d\theta = \frac{\pi}{8} \log 2$.
5. Evaluate $\int (\log x)^2 dx$.

